COMENIUS UNIVERSITY IN BRATISLAVA FACULTY OF MATHEMATICS, PHYSICS AND INFORMATICS

CHARACTERIZING MALWARE SAMPLES IN THE SOREL-20M DATASET BY CONCEPT LEARNING BACHELOR THESIS

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Abstrakt

Slovenský abstrakt v rozsahu 100-500 slov, jeden odstavec. Abstrakt stručne sumarizuje výsledky práce. Mal by byť pochopiteľný pre bežného informatika. Nemal by teda využívať skratky, termíny alebo označenie zavedené v práci, okrem tých, ktoré sú všeobecne známe.

Kľúčové slová: jedno, druhé, tretie (prípadne štvrté, piate)

Abstract

Abstract in the English language (translation of the abstract in the Slovak language).

Keywords:

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Chapter 1

Introduction

The immense technological advances we had a chance to witness in the past few decades has gradually enabled us to perform many of the previously implausible computationally-intensive tasks in near real time. As a consequence, various artificial-intelligence (AI) methods have been successfully applied in a number of areas where data is abundant.

Although the cyber-security industry can certainly be considered a field belonging into this category, the research regarding malware detection is still conducted predominantly by the commercial sector and the details are often highly confidential. This is due in part to the lack of sufficiently-large publicly-available data sets. Fortunately, in the recent years, a few such sources of information have emerged, e.g. the EMBER [1] and SOREL-20M [14] data sets.

While machine-learning (ML) techniques have long been used in the proprietary tools to protect a user's system against misbehaving software [3], there have been only few attempts to employ symbolic AI to malware detection (for instance, ...). Hence, our main objective is to empirically evaluate the performance of one novel symbolic approach to inductive learning, i.e. learning from examples, called concept learning.

As its name suggests, a concept-learning algorithm in general endeavours to find the most precise descriptions of the given set of positive examples based on the provided knowledge. We will use these algorithms to obtain possible characterisations of malware deduced from the information acquired via static analysis of both malicious and benign files. These data will be extracted from EMBER and SOREL-20M. Since the outcome of a concept-learning process is a human-readable logical formula, we expect to achieve better explainability of malware classification in comparison with the standard statistical methods.

In addition, we propose several changes to the algorithms selected for evaluation. Despite having been tested only in this specific scenario, we believe that the applying our modifications can lead to relevant improvements in other situations as well. We will also justify their relevance formally.

In the remainder of this document, we first discuss \dots

Chapter 2

Description Logics and OWL

Description Logics (DLs) were introduced in the late 1980s as a new family of logical formalisms specifically designed for structured knowledge representation in an effort to automate reasoning over vast amounts of knowledge [4].

Inspired by human conceptual thinking, description logics (DLs) provide us with instruments to classify entities, identify binary relationships between them, and create hierarchies over the classes and associations. Using these tools, we can model the knowledge of an application domain. We refer to such representations as *knowledge bases* in the context of DLs.

Although most of the DLs are essentially fragments of first-order logic (FOL), the theory behind them was carefully developed so that reasoning in DLs, unlike in FOL, remains decidable [20], which is, of course, crucial for automation.

The whole DL family comprises a number of formalisms, differing mainly in the level of expressivity stemming from the richness of syntax. Here, we present the \mathcal{SROIQ} DL and OWL 2 DL.

$2.1 \quad \mathcal{SROIQ} \text{ DL}$

The SROIQ DL [15] is among the most expressive DLs. The next two sections deal with its syntax and semantics, respectively. The definitions we provide in these sections are based on Rudoplh's [20] and Baader et al.'s [4] treatises.

2.1.1 Syntax

As in any logical formalism, we first need to specify a set of distinguishable symbols (vocabulary) in order to define a language in which meaningful sentences (statements) can be formed, possibly with use of connectors and modifiers. In DLs, we have concept names, role names, and individual names that together determine a language's vocabulary.

Definition 1 (Vocabulary). The **vocabulary** of a SROIQ language \mathcal{L} is a triple $\Sigma = (N_R, N_C, N_I)$, where N_R is a set of **role names**, N_C a set of **concept names**, and N_I a set of **individual names**. The sets N_R, N_C, N_I are mutually disjoint. None of the symbols in $\{\top, \bot, \neg, \sqcap, \sqcup, \exists, \forall, \text{Self}, \geq, \leq, \circ\}$ and punctuation symbols appears in N_R, N_C , or N_I .

Intuitively, we use concept names to denote categories, such as Person, Animal, or Laptop, role names as identifiers of binary relationships, e.g., worksAt, livesIn, or manufacturedBy, and individual names to refer to particular entities, for example, john, cat_alice, or bobs_newest_ultrabook.

Given the vocabulary of a \mathcal{SROIQ} language, we can clearly define what constructs are considered valid in that language. However, contrary to monolithic theories in FOL, knowledge bases in \mathcal{SROIQ} are split into three parts: assertional (ABox), terminological (TBox), and relational (RBox). Since each of them has a different purpose, we need to treat the syntax of ABox, TBox, and RBox statements separately.

RBox

The main component of an RBox is the *role hierarchy*, which enables us to define how the binary relationships are connected to one another.

Definition 2 (Roles and Role Inversion). Let \mathcal{L} be a \mathcal{SROIQ} language. The set of all roles in \mathcal{L} is the set $\mathbf{R} = \{r \mid r \in N_R\} \cup \{r^- \mid r \in N_R\} \cup \{u\}$, where u denotes the universal role.

For any $r \in N_R$, the role r^- is called the **inverse role** of r. The function of role inversion Inv: $\mathbf{R} \to \mathbf{R}$ is defined for all $r \in \mathbf{R}$ as follows:

$$\operatorname{Inv}(r) = \begin{cases} r^-, & \text{if } r \in N_R, \\ s, & \text{if } r = s^-, \text{ for some } s \in N_R, \\ u, & \text{if } r = u. \end{cases}$$

Definition 3 (Role Inclusion Axioms and Role Hierarchies). Let \mathcal{L} be a \mathcal{SROIQ} language. A role inclusion axiom (RIA) is any statement of the form $r_1 \circ r_2 \circ \cdots \circ r_n \sqsubseteq r$, where $n \in \mathbb{Z}^+$ and $r_1, r_2, \ldots, r_n, r \in \mathbf{R}$. For any $r, s \in \mathbf{R}$, we call the RIA $r \sqsubseteq s$ a simple role inclusion and r a subrole of s.

A role hierarchy (\mathcal{H}_R) is any finite set of RIAs.

For decidability of reasoning in \mathcal{SROIQ} , it is inevitable that the role hierarchy in an RBox is regular [20].

Definition 4 (Simple and Non-Simple Roles). Let \mathcal{L} be a SROIQ language and \mathcal{H}_R be a role hierarchy in \mathcal{L} . The set \mathbf{R}^n of all non-simple roles in \mathcal{L} w.r.t. \mathcal{H}_R is the smallest set for which each of the following conditions holds:

2.1. SROIQ DL 5

- if $r_1 \circ r_2 \circ \cdots \circ r_n \sqsubseteq r \in \mathcal{H}_R$, for n > 1 and any $r_1, r_2, \ldots, r_n, r \in \mathbf{R}$, then $r \in \mathbf{R}^n$,
- if $r, s \in \mathbf{R}$, $r \in \mathbf{R}^n$, and $r \sqsubseteq s \in \mathcal{H}_R$, then $s \in \mathbf{R}^n$,
- if $r \in \mathbf{R}^n$, then $\operatorname{Inv}(r) \in \mathbf{R}^n$.

The set of all simple roles in \mathcal{L} w.r.t. \mathcal{H}_R is the set $\mathbf{R}^s = \mathbf{R} \setminus \mathbf{R}^n$.

Definition 5 (Regular Role Hierarchy). Let \mathcal{L} be a SROIQ language and \mathcal{H}_R be a role hierarchy in \mathcal{L} . The **role hierarchy** \mathcal{H}_R **is regular** if there exists a strict partial order¹ \prec on \mathbb{R}^n such that $r \prec s$ iff $Inv(r) \prec s$, for any $r, s \in \mathbb{R}^n$, and each RIA in \mathcal{H}_R has one of the following forms:

- $r \circ r \sqsubseteq r$,
- $\operatorname{Inv}(r) \sqsubseteq r$,
- $s_1 \circ s_2 \circ \cdots \circ s_n \sqsubseteq r$,
- $r \circ s_1 \circ s_2 \circ \cdots \circ s_n \sqsubseteq r$,
- $s_1 \circ s_2 \circ \cdots \circ s_n \circ r \sqsubseteq r$,

where $n \in \mathbb{Z}^+$, $r \in N_R$, $s_1, s_2, \ldots, s_n \in \mathbf{R}$, with $s_i \prec r$, for every non-simple role s_i , where $i = 1, 2, \ldots, n$.

The rest of the RBox consists of statements through which we can express that some roles have additional properties, such as reflexivity or symmetry. We collectively call these statements role characteristics.

Definition 6 (Role Characteristics). Let \mathcal{L} be a SROIQ language and \mathcal{H}_R be a role hierarchy in \mathcal{L} . A role characteristic is any statement of one of the following forms: Ref(r) (reflexivity), Irref(r) (irreflexivity), Sym(r) (symmetry), Asym(r) (asymmetry), or Disj(s, s') (disjointness), for any $r \in \mathbf{R}$ and $s, s' \in \mathbf{R}^s$.

A \mathcal{SROIQ} RBox can be thus formally defined as follows.

Definition 7 (RBox). Let \mathcal{L} be a SROIQ language. A SROIQ **RBox** is any set $\mathcal{R} = \mathcal{H}_R \cup \operatorname{Char}_R$, where \mathcal{H}_R is a regular role hierarchy and Char_R is a finite set of role characteristics.

TBox

The terminological part of a knowledge base predominantly allows us to create a complex hierarchy over the set of categories we denote by concept names.

Definition 8 (Concept Expressions). Let \mathcal{L} be a SROIQ language and \mathcal{R} be an RBox in \mathcal{L} . The set \mathbf{C} of all concept expressions (concepts) in \mathcal{L} w.r.t. \mathcal{R} is the smallest set for which each of the following conditions is satisfied:

• every concept name $C \in N_C$ is an element of \mathbf{C} (atomic concept),

 $^{^1\}mathrm{A}$ strict partial order is a transitive and asymmetric binary relation.

- the concepts \top (top concept) and \bot (bottom concept) belong to \mathbb{C} ,
- $\{a_1, \ldots, a_n\} \in \mathbb{C}$, for any $n \in \mathbb{Z}^+$ and $a_1, \ldots, a_n \in N_I$; the concepts of this form are called **nominals**,
- if $C, D \in \mathbb{C}$, then $\neg C \in \mathbb{C}$ (negation), $C \sqcap D \in \mathbb{C}$ (intersection/conjunction), and $C \sqcup D \in \mathbb{C}$ (union/disjunction),
- if $r \in \mathbf{R}$ and $C \in \mathbf{C}$, then $\exists r.C \in \mathbf{C}$ (existential quantification), and $\forall r.C \in \mathbf{C}$ (universal quantification),
- if $r \in \mathbb{R}^s$, then $\exists r. \text{Self} \in \mathbb{C}$ (self restriction),
- if $r \in \mathbb{R}^s$, $C \in \mathbb{C}$, and $n \in \mathbb{N}^2$, then $\geq n$ $r.C \in \mathbb{C}$ (at-least restriction), and $\leq n$ $r.C \in \mathbb{C}$ (at-most restriction); these are also jointly called cardinality constraints.

Definition 9 (General Concept Inclusion Axioms and TBox). Let \mathcal{L} be a SROIQ language and \mathcal{R} be an RBox in \mathcal{L} . A general concept inclusion axiom (GCI) is any statement of the form $C \sqsubseteq D$, where $C, D \in \mathbb{C}$, read "C is subsumed by D", "C is a subconcept of D", or "D is a superconcept of C".

A SROIQ **TBox** (T) is any finite set of GCIs.

ABox

An ABox serves as a tool to express facts about named individuals inside the model of the world built via the RBox and TBox.

Definition 10 (Individual Assertions and ABox). Let \mathcal{L} be a \mathcal{SROIQ} language, \mathcal{R} be an RBox in \mathcal{L} , and \mathcal{T} be a TBox in \mathcal{L} . An individual assertion is a statement in any of the following forms: C(a) (concept assertion), r(a,b) (role assertion), $\neg r(a,b)$ (negated role assertion), $a \approx b$ (equality statement), or $a \approx b$ (inequality statement), where $C \in \mathbb{C}$, $r \in N_R$, and $a, b \in N_I$.

A SROIQ ABox (A) is any finite set of individual assertions.

Knowledge Base

As we mentioned earlier, a SROIQ knowledge base is simply a union of an ABox, TBox, and RBox.

Definition 11 (Knowledge Base). Let \mathcal{L} be a SROIQ language. A SROIQ knowledge base is any set $\mathcal{K} = \mathcal{R} \cup \mathcal{T} \cup \mathcal{A}$, where $\mathcal{R}, \mathcal{T}, \mathcal{A}$ are an RBox, a TBox, and an ABox in \mathcal{L} , respectively.

Before we move on to the semantics of SROIQ, we will look at one example of a SROIQ knowledge base to better grasp how the knowledge described by sentences in a natural language is converted into a knowledge base.

 $^{^2}$ We assume that zero is a natural number as well.

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Example 1 (Knowledge Base). Imagine we would like to translate the English sentences S_1, \ldots, S_7 given below into SROIQ statements and create a knowledge base.

 S_1 : One is a parent of somebody else if and only if the latter is a child of the former.

 S_2 : If someone is a parent of another parent, then the first is a grandparent of all the children the second has.

 S_3 : No one is a parent of themselves.

 S_4 : Every man is a person.

S₅: A happy person is either a man with no child or a person who has at least two children.

 S_6 : Alice is a parent of Bob.

 S_7 : Chris is a happy person.

To accomplish this task, we first define a SROIQ language $\mathcal L$ with

```
N_R = \{ 	ext{parentOf}, 	ext{childOf}, 	ext{grandparentOf} \}, \ N_C = \{ 	ext{Person}, 	ext{Man}, 	ext{HappyPerson} \}, \ N_I = \{ 	ext{Alice}, 	ext{Bob}, 	ext{Chris} \}.
```

The sentences S_1, \ldots, S_7 can be then transformed into the statements $S_{1.1}^{\mathcal{L}}, S_{1.2}^{\mathcal{L}}, S_2^{\mathcal{L}}, \ldots, S_7^{\mathcal{L}}$ in \mathcal{L} as follows:

```
S_{1.1}^{\mathcal{L}}: parentOf \sqsubseteq childOf^-, S_{1.2}^{\mathcal{L}}: childOf \sqsubseteq parentOf^-, S_{2}^{\mathcal{L}}: parentOf \circ parentOf \sqsubseteq grandparentOf, S_{3}^{\mathcal{L}}: Irref(parentOf), S_{4}^{\mathcal{L}}: Man \sqsubseteq Person, S_{5}^{\mathcal{L}}: HappyPerson \sqsubseteq (Man \sqcap \forallparentOf.\bot) \sqcup (Person \sqcap \geq 2 parentOf.\top), S_{6}^{\mathcal{L}}: parentOf(Alice, Bob), S_{7}^{\mathcal{L}}: HappyPerson(Chris),
```

where $S_{1.1}^{\mathcal{L}}, S_{1.2}^{\mathcal{L}}, S_2^{\mathcal{L}}, S_3^{\mathcal{L}}$ together constitute an RBox \mathcal{R} , $S_4^{\mathcal{L}}, S_5^{\mathcal{L}}$ form a TBox \mathcal{T} , and $S_6^{\mathcal{L}}, S_7^{\mathcal{L}}$ represent an ABox \mathcal{A} . The corresponding knowledge base \mathcal{K} would thus be a union of \mathcal{R}, \mathcal{T} and \mathcal{A} , i.e., $\mathcal{K} = \{S_{1.1}^{\mathcal{L}}, S_{1.2}^{\mathcal{L}}, S_2^{\mathcal{L}}, \dots, S_7^{\mathcal{L}}\}$.

2.1.2 Semantics

Knowing the rules for writing statements in \mathcal{SROIQ} and understanding their intended use, we can discuss their formal semantics in detail, i.e., how we interpret them and investigate whether they are satisfied.

Interpretations

Since every knowledge base is merely an abstraction of the world it tries to model, we need to define the way we will materialize this abstraction given a set of entities. In DLs, this need is fulfilled by *interpretations*.

Definition 12 (Interpretation). Let \mathcal{L} be a SROIQ language. An interpretation is a pair $\mathcal{I} = (\Delta^{\mathcal{I}}, \cdot^{\mathcal{I}})$, where $\Delta^{\mathcal{I}}$ is a non-empty set, called domain, and $\cdot^{\mathcal{I}}$ is an interpretation function which maps

- each $a \in N_I$ to an element $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$ (individual),
- each $C \in N_C$ to a subset $C^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$ (concept extension),
- each $r \in N_R$ to a subset $r^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$ (role extension).

The interpretation function $\cdot^{\mathcal{I}}$ is then extended to all \mathcal{SROIQ} roles and concepts as follows:

- $u^{\mathcal{I}} = \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$.
- $\bullet \ (r^-)^{\mathcal{I}} = \{ (\delta, \hat{\delta}) \in \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}} \mid (\hat{\delta}, \delta) \in r^{\mathcal{I}} \},$
- $T^{\mathcal{I}} = \Delta^{\mathcal{I}}, \ \bot^{\mathcal{I}} = \emptyset,$
- $(\neg C)^{\mathcal{I}} = \Delta^{\mathcal{I}} \setminus C^{\mathcal{I}}$,
- $\{a_1, a_2, \dots, a_k\}^{\mathcal{I}} = \{a_1^{\mathcal{I}}, a_2^{\mathcal{I}}, \dots, a_k^{\mathcal{I}}\},\$
- $(C \sqcap D)^{\mathcal{I}} = C^{\mathcal{I}} \cap D^{\mathcal{I}}, (C \sqcup D)^{\mathcal{I}} = C^{\mathcal{I}} \cup D^{\mathcal{I}},$
- $(\exists s.C)^{\mathcal{I}} = \{\delta \mid there \ is \ \hat{\delta} \in \Delta^{\mathcal{I}} \ with \ (\delta, \hat{\delta}) \in s^{\mathcal{I}} \ and \ \hat{\delta} \in C^{\mathcal{I}}\},$
- $(\forall s.C)^{\mathcal{I}} = \{ \delta \mid for \ all \ \hat{\delta} \in \Delta^{\mathcal{I}}, \ if \ (\delta, \hat{\delta}) \in s^{\mathcal{I}}, \ then \ \hat{\delta} \in C^{\mathcal{I}} \},$
- $(\exists s. Self)^{\mathcal{I}} = \{ \delta \mid (\delta, \hat{\delta}) \in s^{\mathcal{I}} \},$
- $(\geq n \ t.C)^{\mathcal{I}} = \{\delta \mid |\{\hat{\delta} \in \Delta^{\mathcal{I}} \mid (\delta, \hat{\delta}) \in t^{\mathcal{I}} \ and \ \hat{\delta} \in C^{\mathcal{I}}\}| \geq n\},$
- $(\leq n \ t.C)^{\mathcal{I}} = \{\delta \mid |\{\hat{\delta} \in \Delta^{\mathcal{I}} \mid (\delta, \hat{\delta}) \in t^{\mathcal{I}} \ and \ \hat{\delta} \in C^{\mathcal{I}}\}| \leq n\},$

for all $r \in N_R$, $s \in \mathbf{R}$, $t \in \mathbf{R}^s$, $C, D \in \mathbf{C}$, $a_1, a_2, \ldots, a_k \in N_I$, $k \in \mathbb{Z}$, and $n \in \mathbb{N}$.

Every individual $\delta \in C^{\mathcal{I}}$ is called an **instance** of C. If $(\delta, \hat{\delta}) \in r^{\mathcal{I}}$, then we say that $\hat{\delta}$ is an **r-filler** of δ in \mathcal{I} .

For illustration, we will examine one model of the knowledge base constructed in Example 1.

Example 2 (Interpretation). Let \mathcal{L} be the \mathcal{SROIQ} language and \mathcal{K} be the knowledge base in \mathcal{L} defined in Example 1. Now, let us take the interpretation $\mathcal{I} = (\Delta^{\mathcal{I}}, \mathcal{I})$ where

$$\Delta^{\mathcal{I}} = \{A, B, C, D, E, F\},$$

$$\mathtt{Alice}^{\mathcal{I}} = A, \quad \mathtt{Bob}^{\mathcal{I}} = B, \quad \mathtt{Chris}^{\mathcal{I}} = C,$$

$$\mathtt{Person}^{\mathcal{I}} = \{A, B, C, D\}, \quad \mathtt{Man}^{\mathcal{I}} = \{B, C, D\}, \quad \mathtt{HappyPerson}^{\mathcal{I}} = \{A, C, D\},$$

$$\mathtt{parentOf}^{\mathcal{I}} = \{(A, B), (A, D), (E, F)\}, \quad \mathtt{childOf}^{\mathcal{I}} = \{(B, A), (D, A), (F, E)\},$$

$$\mathtt{grandparentOf}^{\mathcal{I}} = \{(E, F)\}.$$

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Apparently, \mathcal{I} is a model of \mathcal{K} by Definition 12. Note that not every individual in $\Delta^{\mathcal{I}}$ has to be named, that is, there can be $\delta \in \Delta^{\mathcal{I}}$ for which no $a \in N_I$ exists such that $a^{\mathcal{I}} = \delta$ (for instance, D). Conversely, we could re-define \mathcal{I} so that $\mathsf{Bob}^{\mathcal{I}} = \mathsf{Chris}^{\mathcal{I}} = B$. Of course, when an individual from $\Delta^{\mathcal{I}}$ is identified by more than one individual name, all individual assertions referring to any of these individual names apply to such individual. Looking at the definition of $\cdot^{\mathcal{I}}$, we can also see the importance of diligence in modeling, since for example in \mathcal{I} , E is simultaneously a parent and a grandparent of F, which is possible due to the fact that \mathcal{K} does not require the disjointness of parentOf and grandparentOf.

Seeing how interpretations work, it slowly becomes evident that apart from building a concept hierarchy, we are also able to define various constraints with the help of GCIs. For instance, we can assert that all individuals related to another individual (or to themselves) via a given role r have to be instances of a particular concept, called domain and referred to as dom(r). Returning back to Example 1, to set the domain of the role parentOf to Person, that is, to tell that all parents have to be people, we would use the statement

$$\neg Person \sqcap \exists parentOf. \top \sqsubseteq \bot.$$

Analogously, it is possible to restrict the range of r, i.e., to state that every individual to which any individual is connected through r must be an instance of a specific concept, denoted rng(r). To give an example, we may express that the range of the role parentOf has to be Person, or equivalently, that one can only be a parent of a person, as follows:

$$\exists parentOf. \neg Person \sqsubseteq \bot.$$

Satisfaction of Statements

Determining if a statement is true is always bound to a specific interpretation, as this process corresponds to examining whether a particular instance of the world conforms to certain constraints. Therefore, the definition of *statement satisfaction* also depends on the provided interpretation.

Definition 13 (Statement Satisfaction). Let \mathcal{L} be a SROIQ language and \mathcal{I} be an interpretation. The relation "the interpretation \mathcal{I} satisfies a statement α " ($\mathcal{I} \models \alpha$) is given by the following definition:

- $\mathcal{I} \vDash r_1 \circ r_2 \circ \cdots \circ r_n \sqsubseteq r \text{ iff } \{(\delta_0, \delta_n) \in \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}} \mid \text{ there exist } \delta_1, \delta_2, \dots, \delta_{n-1} \in \Delta^{\mathcal{I}} \text{ such that } (\delta_{i-1}, \delta_i) \in r_i^{\mathcal{I}}, \text{ for } i = 1, 2, \dots, n\} \subseteq r^{\mathcal{I}},$
- $\mathcal{I} \models \operatorname{Ref}(r) \text{ iff } \{(\delta, \delta) \mid \delta \in \Delta^{\mathcal{I}}\} \subseteq r^{\mathcal{I}},$
- $\mathcal{I} \vDash \operatorname{Irref}(r) \text{ iff } \{(\delta, \delta) \mid \delta \in \Delta^{\mathcal{I}}\} \cap r^{\mathcal{I}} = \emptyset,$

- $\mathcal{I} \vDash \operatorname{Sym}(r)$ iff it holds that $(\delta, \hat{\delta}) \in r^{\mathcal{I}}$ implies $(\hat{\delta}, \delta) \in r^{\mathcal{I}}$, for any $\delta, \hat{\delta} \in \Delta^{\mathcal{I}}$,
- $\mathcal{I} \vDash \operatorname{Asym}(r)$ iff it holds that $(\delta, \hat{\delta}) \in r^{\mathcal{I}}$ implies $(\hat{\delta}, \delta) \notin r^{\mathcal{I}}$, for any $\delta, \hat{\delta} \in \Delta^{\mathcal{I}}$,
- $\mathcal{I} \vDash \text{Disj}(s, t) \text{ iff } s^{\mathcal{I}} \cap t^{\mathcal{I}} = \emptyset,$
- $\mathcal{I} \vDash C \sqsubseteq D \text{ iff } C^{\mathcal{I}} \subseteq D^{\mathcal{I}},$
- $\mathcal{I} \vDash C(a)$ iff $a^{\mathcal{I}} \in C^{\mathcal{I}}$,
- $\mathcal{I} \vDash r(a,b)$ iff $(a^{\mathcal{I}}, b^{\mathcal{I}}) \in r^{\mathcal{I}}$,
- $\mathcal{I} \vDash \neg r(a, b) \text{ iff } (a^{\mathcal{I}}, b^{\mathcal{I}}) \notin r^{\mathcal{I}},$
- $\mathcal{I} \vDash a \approx b \text{ iff } a^{\mathcal{I}} = b^{\mathcal{I}},$
- $\mathcal{I} \vDash a \approx b \text{ iff } a \neq b$,

where $r_1, r_2, \ldots, r_n, r \in \mathbf{R}$, $s, t \in \mathbf{R}^s$, $C \in \mathbf{C}$, $a, b \in N_I$, and $n \in \mathbb{Z}$.

The interpretation \mathcal{I} satisfies (is a **model** of) a knowledge base \mathcal{K} ($\mathcal{I} \models \mathcal{K}$) if it satisfies all statements in \mathcal{K} .

The notation $\mathcal{I} \not\models \alpha$ ($\mathcal{I} \not\models \mathcal{K}$) indicates that the interpretation \mathcal{I} does not satisfy the statement α (the knowledge base \mathcal{K}).

Entailment

Having acquired some knowledge, we usually seek to make new inferences from this knowledge. In order to have a formal apparatus to verify that our observations logically follow from a knowledge base, we define the notion of *entailment*.

Definition 14 (Entailment). Let \mathcal{L} be a SROIQ language and \mathcal{K} be a knowledge base in \mathcal{L} . We say that the **knowledge base** \mathcal{K} **entails a statement** α ($\mathcal{K} \models \alpha$) if for all interpretations \mathcal{I} , it is true that if $\mathcal{I} \models \mathcal{K}$, then $\mathcal{I} \models \alpha$.

The knowledge base K entails a set of statements S ($K \models S$) if it entails each statement in S. The notation $K \not\models \alpha$ ($K \not\models S$) indicates that the knowledge base K does not entail the statement α (the set of statements S).

Logical Equivalence and Strict Subsumption

We conclude the section on SROIQ semantics with the definitions of logical equivalence and strict subsumption, which are convenient ways to detect likeness of two concepts or roles and exclude such pairs from the relation of subsumption, respectively.

Definition 15 (Logical Equivalence). Let \mathcal{L} be a \mathcal{SROIQ} language and \mathcal{K} be a knowledge base in \mathcal{L} . Concepts $C, D \in \mathbf{C}$ are logically equivalent w.r.t. \mathcal{K} ($\mathcal{K} \models C \equiv D$) if and only if $\mathcal{K} \models \{C \sqsubseteq D, D \sqsubseteq C\}$. Roles $r, s \in \mathbf{R}$ are logically equivalent w.r.t. \mathcal{K} ($\mathcal{K} \models r \equiv s$) if and only if $\mathcal{K} \models \{r \sqsubseteq s, s \sqsubseteq r\}$.

If in addition $K = \emptyset$, the concepts C, D (roles r, s) are said to be logically equivalent, denoted $C \equiv D$ ($r \equiv s$).

2.2. OWL 2 DL

Definition 16 (Strict Subsumption). Let \mathcal{L} be a \mathcal{SROIQ} language and \mathcal{K} be a knowledge base in \mathcal{L} . A **concept** $C \in \mathbf{C}$ is **strictly subsumed** by a concept $D \in \mathbf{C}$ w.r.t. \mathcal{K} ($\mathcal{K} \models C \sqsubseteq D$) if and only if $\mathcal{K} \models \{C \sqsubseteq D\}$ and $\mathcal{K} \not\models C \equiv D$. A **role** $r \in \mathbf{R}$ is **strictly subsumed** by a role $s \in \mathbf{R}$ w.r.t. \mathcal{K} ($\mathcal{K} \models r \sqsubseteq s$) if and only if $\mathcal{K} \models \{r \sqsubseteq s\}$ and $\mathcal{K} \not\models r \equiv s$.

If $K \vDash C \sqsubset D$, where $C, D \in \{\top\} \cup N_C$, and there exists no $E \in \mathbb{C}$ such that $K \vDash C \sqsubset E$ and $K \vDash E \sqsubset D$, we call C a **direct subconcept** of D. If $K \vDash r \sqsubset s$, where $r, s \in \{u\} \cup N_R$, and there exists no $t \in \mathbb{C}$ such that $K \vDash r \sqsubset t$ and $K \vDash t \sqsubset s$, we call r a **direct subrole** of s.

2.2 OWL 2 DL

The OWL 2 DL [13] is a member of the family of OWL ontology languages, which were proposed by the World Wide Web Consortium (W3C) to back the Semantic Web initiative [2] – an initiative for a next-generation Web where information is semantically organized. Since then, OWL ontology languages have been used in a wide range of areas apart from the Semantic Web, where automated reasoning and semantic retrieval helps with organization of large amounts of data (e.g., medicine [8] or energy management [9]). Ontology languages in general were and still are evolving alongside DLs as a means of structured knowledge representation. Some ontology languages, such as the OWL 2 DL, even take DLs as their formal bases. More precisely, the OWL 2 DL is based on the \mathcal{SROIQ} DL and is essentially its extension. For example, OWL 2 adds the support for data types, so the role fillers can be numbers, strings, etc. There are also several extra-logical features OWL 2 provides beyond the standard DL tools, e.g., annotations. Lastly, the OWL 2 syntax differs from the discussed \mathcal{SROIQ} syntax as well, resulting from the slightly different origins of ontology languages and DLs.

Table 2.1: Comparison of DL and OWL terminology.

DLs	OWL
knowledge base	ontology
concept	class
role	object property
data-type role	data property
top concept	owl:Thing
bottom concept	owl:Nothing
universal role	owl:topObjectProperty
universal data-type role	owl:topDataProperty

In our research, we use an OWL 2 DL ontology (a knowledge base in effect, see Table 2.1) to represent data but the extensions of \mathcal{SROIQ} are not yet utilized and all OWL 2 statements we will present can and will be written in the \mathcal{SROIQ} syntax. Therefore, we do not go into the details about OWL 2 and its connection to \mathcal{SROIQ} , which is, however, thoroughly covered in [4] and [20]. Nevertheless, we introduce a bit of OWL terminology by linking the most fundamental OWL terms to their respective DL counterparts in Table 2.1. We will use the DL terminology in the chapters related closely to DLs, i.e., Chapters 3 and 5, and the OWL nomenclature elsewhere.

Chapter 3

Learning in Description Logics

Since DLs, especially those supporting role hierarchies, give us the ability to capture various aspects of an application domain, one may choose from several learning objectives to pursue. In this section, we thus first define the DL learning problem a solution to which we aim to find in malware detection. Next, we present the approach to this problem that we decided to employ, together with the selected algorithms.

3.1 Concept-Learning Problem

In our research, we focus on solving the problem of learning concept expressions, which we define below [17].

Definition 17 (Concept-Learning Problem). Let \mathcal{L} be a DL language and \mathcal{K} be a knowledge base in \mathcal{L} . Let $E^+ \subseteq N_I$ be a set of positive examples and $E^- \subseteq N_I$ be a set of negative examples, with $E^+ \cap E^- = \emptyset$.

Given K, E^+ , and E^- , find a concept expression $C \in \mathbb{C}$, also called a description, such that both of the following conditions are satisfied:

$$\mathcal{K} \vDash C(a), \text{ for all } a \in E^+,$$
 (3.1)

$$\mathcal{K} \vDash \neg C(a), \text{ for all } a \in E^-.$$
 (3.2)

If $K \vDash C(a)$ holds for some $a \in E^+ \cup E^-$ and $C \in \mathbb{C}$, we say that C covers a.

This definition can be interpreted as follows: Given some background knowledge and two sets of individuals, positive and negative examples, respectively, the goal of concept learning is to use the background knowledge to find a minimal description of the positive examples, where minimality is achieved by ensuring that none of the negative examples fits the description.

Notice that we always supply additional information about which instances are positive and which are negative, in other words, the learning is supervised. There is

also an adaptation of the above definition that allow unlabeled examples as well. This is useful for learning under the *open-world assumption*, i.e., when we do not conclude that a certain observation is false if it does not follow from the knowledge base. Despite relying on the open-world assumption is a common practice in the field of knowledge representation, for our use case, it is more convenient to work under the opposite – the *closed-world assumption*.

3.2 Concept Learning Using Refinement Operators

Definition 17 states that a concept learning problem is considered to be solved once an appropriate description of positive examples is found. Hence, it is possible to cast this problem to a search problem, with the search space being simply the space of all valid concept expressions. One of the approaches to order the elements of this search space is to exploit the standard DL relation of subsumption [17]. Such successor functions are called *refinement operators*.

Definition 18 (Refinement Operator). Let \mathcal{L} be a DL language and \mathcal{K} be a knowledge base in \mathcal{L} with no ABox. A mapping $\rho : \mathbb{C} \to 2^{\mathbb{C}}$ is a **downward (upward)** refinement operator in the quasi-ordered space $(\mathcal{L}, \sqsubseteq)$ if for all $C \in \mathbb{C}$, it holds that $D \in \rho(C)$ implies $\mathcal{K} \vDash D \sqsubseteq C$ ($\mathcal{K} \vDash C \sqsubseteq D$). The concept D is called a refinement of C and more specifically, a specialization (generalization) of C.

For example, if we let \rightsquigarrow denote a single refinement operation, one branch of a search tree induced by a downward refinement operator may have the following form (with the leftmost concept being in the root node and the rightmost in the leaf node):

$$\top \leadsto \forall r. \top \leadsto \forall r. C \leadsto (\forall r. C) \sqcap D. \tag{3.3}$$

We refer to such a sequence of refinement operations as a *refinement chain*. Usually, the downward-refinement process starts from the most-generic concept, i.e., the top concept, which has the maximum potential to specialize.

In our research, we study the suitability of concept-learning algorithms utilizing the refinement operator called simply ρ . In the next two sections, we first present the definition of this operator and then discuss the examined algorithms and their peculiarities.

3.2.1 The ρ Refinement Operator

Proposed by Lehmann and Hitzler [17], the ρ refinement operator was the first operator for solving the concept-learning problem in DLs. Before we formally define ρ , it is inevitable to introduce several auxiliary notions.

¹A quasi-order is a reflexive and transitive binary relation.

To move through the subsumption hierarchies created over the sets of concept names and role names, we need functions for crawling them both in the upward $(\operatorname{sh}^{\mathbf{C}}_{\uparrow} \operatorname{and} \operatorname{sh}^{\mathbf{R}}_{\uparrow})$ and downward $(\operatorname{sh}^{\mathbf{C}}_{\downarrow} \operatorname{and} \operatorname{sh}^{\mathbf{R}}_{\downarrow})$ direction.

Definition 19 (Subsumption Hierarchy Crawlers). Let \mathcal{L} be a DL language and \mathcal{K} be a knowledge base in \mathcal{L} with an ABox \mathcal{A} . Let $\mathcal{K}' = \mathcal{K} \setminus \mathcal{A}$. We define the functions $\operatorname{sh}_{\uparrow}^{\mathbf{C}} : \{\top\} \cup N_C \to 2^{\{\top\} \cup N_C} \text{ and } \operatorname{sh}_{\downarrow}^{\mathbf{C}} : \{\top\} \cup N_C \to 2^{\{\top\} \cup N_C} \text{ for all } C \in \{\top\} \cup N_C \text{ as follows:}$

$$\operatorname{sh}^{\mathbf{C}}_{\uparrow}(C) = \{ D \in \{\top\} \cup N_C \mid \mathcal{K}' \vDash C \sqsubset D \text{ and } C \text{ is a direct subconcept of } D \text{ w.r.t. } \mathcal{K}' \},$$

 $\operatorname{sh}^{\mathbf{C}}_{\downarrow}(C) = \{ D \in \{\top\} \cup N_C \mid \mathcal{K}' \vDash D \sqsubset C \text{ and } C \text{ is a direct subconcept of } D \text{ w.r.t. } \mathcal{K}' \}.$

The functions $\operatorname{sh}_{\uparrow}^{\mathbf{R}}: \{u\} \cup N_R \to 2^{\{u\} \cup N_R} \text{ and } \operatorname{sh}_{\downarrow}^{\mathbf{R}}: \{u\} \cup N_R \to 2^{\{u\} \cup N_R} \text{ map each } r \in \{u\} \cup N_R \text{ to the sets below:}$

$$\operatorname{sh}^{\mathbf{R}}_{\uparrow}(r) = \{ s \in \{u\} \cup N_R \mid \mathcal{K}' \vDash r \sqsubseteq s \text{ and } r \text{ is a direct subrole of } s \text{ w.r.t. } \mathcal{K}' \},$$

 $\operatorname{sh}^{\mathbf{R}}_{\downarrow}(r) = \{ s \in \{u\} \cup N_R \mid \mathcal{K}' \vDash s \sqsubseteq r \text{ and } s \text{ is a direct subrole of } r \text{ w.r.t. } \mathcal{K}' \}.$

The presence of domain and range assertions facilitates the ρ operator to avoid generating refinements that certainly do not cover any individual because they do not satisfy a domain or range restriction. However, ρ was designed to work only with *atomic domains* and *ranges*, i.e., those which are either concept names or the top concept.

Definition 20 (Atomic Domains And Ranges). Let \mathcal{L} be a DL language and \mathcal{K} be a knowledge base in \mathcal{L} .

The atomic domain of a role $r \in \mathbf{R}$ is a concept $\operatorname{ad}(r) \in \{\top\} \cup N_C$ such that $\mathcal{K} \models \operatorname{dom}(r) \sqsubseteq \operatorname{ad}(r)$ and there is no $C \in \{\top\} \cup N_C$ with $\mathcal{K} \models \operatorname{dom}(r) \sqsubseteq C$ and $\mathcal{K} \models C \sqsubseteq \operatorname{ad}(r)$.

The atomic range of a role $r \in \mathbf{R}$ is a concept $\operatorname{ar}(r) \in \{\top\} \cup N_C$ such that $\mathcal{K} \models \operatorname{rng}(r) \sqsubseteq \operatorname{ar}(r)$ and there is no $C \in \{\top\} \cup N_C$ with $\mathcal{K} \models \operatorname{rng}(r) \sqsubseteq C$ and $\mathcal{K} \models C \sqsubseteq \operatorname{ar}(r)$.

Conversely, given a concept name, we are able to determine the set of *applicable* role names, whose atomic domains are not disjoint from this concept name, based on the information about domains.

Definition 21 (Applicable Role Names). Let \mathcal{L} be a DL language, \mathcal{K} be a knowledge base in \mathcal{L} , and $C \in \{\top\} \cup N_C$ be a concept. The set of all **applicable role names** for the concept C is the set $\operatorname{app}(C) = \{r \in N_R \mid \mathcal{K} \nvDash \operatorname{ad}(r) \sqcap C \equiv \bot\}$. The set of **the** most general applicable role names for the concept C is the set $\operatorname{mgr}(C) = \{r \in \operatorname{app}(C) \mid \text{there is no } s \in \operatorname{app}(C) \text{ such that } \mathcal{K} \vDash r \sqsubseteq s\}$.

With the above terms defined, we can now, according to [17], formulate the definition of ρ for the \mathcal{SROIQ} DL without nominals and inverse roles, which we omit because the rules for their refinement were not enabled in our experiments.

Definition 22 (The ρ Refinement Operator). Let \mathcal{L} be a DL language and \mathcal{K} be a knowledge base in \mathcal{L} . For any $B \in \{\top\} \cup N_C$, let M_B be the set of all **top-concept** refinements not disjoint from B defined as follows:

$$M_{B} = \{A \mid A \in N_{C}, \mathcal{K} \not\vDash A \sqcap B \equiv \bot, \mathcal{K} \not\vDash A \sqcap B \equiv B, \text{ and}$$

$$there \text{ is no } A' \in N_{C} \text{ such that } \mathcal{K} \vDash A \sqsubset A'\}$$

$$\cup \{\neg A \mid A \in N_{C}, \mathcal{K} \not\vDash \neg A \sqcap B \equiv \bot, \mathcal{K} \not\vDash \neg A \sqcap B \equiv B, \text{ and}$$

$$there \text{ is no } A' \in N_{C} \text{ such that } \mathcal{K} \vDash A' \sqsubset A\}$$

$$\cup \{\exists r. \top \mid r \in \text{mgr}(B)\}$$

$$\cup \{\forall r. \top \mid r \in \text{mgr}(B)\}$$

$$\cup \{\leq \text{mf}(r)r. \top \mid r \in \text{mgr}(B)\},$$

where $\operatorname{mf}(r) = \max_{a \in N_I} |\{b \mid \mathcal{K} \vDash r(a,b)\}|$, for all $r \in N_R$. The **refinement operator** $\rho : \mathbf{C} \to 2^{\mathbf{C}}$ maps every $C \in \mathbf{C}$ to a set

$$\rho(C) = \begin{cases} \{\bot\} \cup \rho_{\top}(C), & \text{if } C = \top, \\ \rho_{\top}(C), & \text{otherwise} \end{cases}$$

where ρ_B is given for each domain of refinement $B \in \{\top\} \cup N_C$ as follows:

$$\label{eq:where ρ_B is given for each domain of refinement $B \in \{\top\} \cup N_C$ as follows:} \\ \begin{cases} \emptyset, & \text{if $C = \bot$}, \\ \bigcup_{m=1}^\infty \{D_1 \sqcup D_2 \sqcup \cdots \sqcup D_m \\ & | D_i \in M_B, \text{ for } i = 1, 2, \ldots, m \}, & \text{if $C = \top$}, \\ \{A' \mid A' \in \operatorname{sh}_+^{\mathbb{C}}(A)\} \\ & \cup \{A \sqcap D \mid D \in \rho_B(\top)\}, & \text{if $C = A$}, \\ \{\neg A' \mid A' \in \operatorname{sh}_+^{\mathbb{C}}(A)\} \\ & \cup \{\neg A \sqcap D \mid D \in \rho_B(\top)\}, & \text{if $C = \lnot A$}, \\ \{\exists r.E \mid E \in \rho_{\operatorname{aur}}(D)\} \\ & \cup \{\exists r.D \mid T \in \operatorname{sh}_+^{\mathbb{C}}(r)\}, & \text{if $C = \lnot A$}, \\ \{\exists r.E \mid E \in \rho_{\operatorname{aur}}(D)\} \\ & \cup \{\exists r.D \mid T \in \operatorname{sh}_+^{\mathbb{C}}(r)\}, & \text{if $C = \lnot T$}, D, \\ \{\forall r.E \mid E \in \rho_{\operatorname{aur}}(D)\} \\ & \cup \{\forall r.D \mid T \in \operatorname{l} E \in \rho_B(\top)\}, & \text{if $C = \lnot T$}, D, \\ \{\geq n. 1 \mid r.D \mid n < \operatorname{mf}(r)\} \\ & \cup \{\geq n. s.E \mid E \in \rho_{\operatorname{aur}}(s)(D)\} \\ & \cup \{(\geq n. s.D) \sqcap E \mid E \in \rho_B(\top)\}, & \text{if $C = \succeq n$} s.D, \\ \{\leq n-1 \mid r.D \mid n > 1\}, & \text{if $C = \lnot n$} s.D, \\ \{C_1 \sqcap \cdots \sqcap C_{i-1} \sqcap D \sqcap C_{i+1} \sqcap \cdots \sqcap C_k, \\ \mid D \in \rho_B(C_i), \text{ for $i = 1, 2, \ldots, k\}}, & \text{if $C = C_1 \sqcap C_2 \sqcap \cdots \sqcap C_k$}, \\ \mid D \in \rho_B(C_i), \text{ for $i = 1, 2, \ldots, k\}}, & \text{if $C = C_1 \sqcup C_2 \sqcup \cdots \sqcup C_k$}, \\ |D \in \rho_B(C_i), \text{ for $i = 1, 2, \ldots, k\}}, & \text{of $C = G_1 \sqcup G_2 \sqcup \cdots \sqcup G_k$}, \\ \text{for any $n \in \mathbb{N}, k \geq 2, A \in N_C, r \in \mathbb{R}, s \in \mathbb{R}^s, C_1, C_2, \ldots, C_k, C, D \in \mathbb{C}.} \\ \text{Intuitively, M_B serves as a basis from which all refinements can be constructed by repeatedly applying a to the obtained concents, starting with T. Although normally.} \end{cases}$$

Intuitively, M_B serves as a basis from which all refinements can be constructed by repeatedly applying ρ to the obtained concepts, starting with \top . Although normally, one would use ρ or ρ_{\top} to get refinements, it might be also beneficial to employ ρ_B directly if we know that all examples we aim to describe are instances of an atomic concept B.

3.2.2 Algorithms

(Toto niekam zaclenit)

We use the implementation of OCEL and CELOE that is a part of DL-Learner [6], a state-of-the-art framework for learning in DLs. This framework also provides the algorithms with a reasoner component responsible for determining whether a given individual is an instance of the provided concept expression.

Throughout our experimentation, we evaluated the performance of four concept-learning algorithms, namely, OCEL, CELOE, ParCEL, and ParCEL-Ex version 2 (hereafter just ParCEL-Ex). To solve the concept-learning problem, each of these algorithms searches the space of all valid concept expressions in a given language ordered by the ρ refinement operator with the guidance of an additional heuristic, assessing mainly how accurate a concept is (exact definition of accuracy is given in Section 6.2). However, notice that the ρ operator is infinite, meaning that there exists a concept C for which the set $\rho(C)$ is not finite (this actually holds for all concepts in the case of ρ). Therefore, the algorithms limit the refinements to only those whose length is lower than or equal to a specified value, where length is defined quite naturally as follows.

...

Using this technique the algorithms can proceed iteratively by revisiting an already searched concept whenever they find it promising based on its heuristic score and gradually asking for longer refinements. The example refinement chain 3.3 demonstrates one such course of action, indeed. The general and substantially simplified procedure is shown in Algorithm 1.

We see that the algorithms allow us to restrict not only the domain in which they search for solutions (D), but also the concept they start with (C). The next input parameter, termination criteria, controls when the learning process is stopped, for instance, after a provided period of time. In Definition 17, we clearly stated what concepts are considered to be solutions, nevertheless, in many real-world situations, it is extremely hard to find perfect descriptions having the there-required properties. For this reason, solution criteria can be changed in order to relax the original definition of a solution. Similarly, less strict minimum-quality criteria enable us to determine a lower bound for the quality of concepts that should be kept in the search tree for further refinement, usually, by enforcing the concepts to cover at least a decent share of the positive examples and/or at most a small number of negative examples. In reality, there is a lot more parameters to tweak and we expand upon the ones whose effects we investigated in our experiments in Section 6.3.

Looking at the actual search process represented by the while loop in Algorithm 1, we have to point out that during the evaluation of the heuristic score at line 14, the coverage of positive and negative examples must be implicitly calculated which

```
Algorithm 1: General concept-learning algorithm using \rho
   Input: a start concept C, a domain of refinement D, termination criteria,
            solution criteria, minimum-quality criteria
   Output: a set of solutions
1 heuristic \leftarrow an algorithm-specific heuristic
2 startNode \leftarrow a new node with
                   parent = none, children = \emptyset, concept = C, length = len(C)
4 searchTree \leftarrow a new tree with startNode as the root and only node
solutions \leftarrow \emptyset
6 while termination criteria are not satisfied do
       node \leftarrow the currently best node from searchTree according to heuristic
 7
       remove node from searchTree
 8
       refinements \leftarrow \{E \in \rho_D(best) \mid node.length - 1 \leq len(E) \leq node.length\}
9
       nodesToAdd \leftarrow \emptyset
10
       foreach E \in refinements do
11
           refNode \leftarrow a \text{ new node with}
12
                         parent = node, children = \emptyset, concept = E, length = len(E)
13
           refNode.score \leftarrow heuristic.evaluate(refNode)
14
           if refNode does not satisfy minimum-quality criteria then
15
               continue
16
           end
17
           node.children \leftarrow node.children \cup \{refNode\}
18
           nodesToAdd \leftarrow nodesToAdd \cup \{refNode\}
19
           if refNode satisfies solution criteria then
20
               solutions \leftarrow solutions \cup \{E\}
\mathbf{21}
           end
22
       end
\mathbf{23}
       node.length \leftarrow node.length + 1
24
       nodesToAdd \leftarrow nodesToAdd \cup \{node\}
25
       add each node from nodesToAdd to searchTree
26
27 end
```

28 return solutions

raises the necessity to have a tool to check if an individual is an instance of a concept (instance checking).

Understanding the learning procedure, we can now discuss the primary characteristics of the algorithms with which we experimented.

OCEL and CELOE

OCEL [17] was the first concept-learning algorithm based on a refinement operator. CELOE [16] was introduced as a variation of OCEL attracted to shorter concepts following the principle of Occam's razor [11], i.e., that simpler descriptions may generalize better since they fit the training conditions more loosely. With OCEL and CELOE, the solution and minimum-quality criteria either coincide (CELOE) or are interrelated (OCEL), and thus only the minimum-quality criteria are configurable. Both of these algorithms were designed to work sequentially in a single thread.

ParCEL and ParCEL-Ex

ParCEL [23] parallelizes the learning process by creating a new worker to execute the instructions at lines 9-26 in Algorithm 1 allowing it to immediately continue and spawn multiple such workers, each responsible for refining a different concept. The maximum number of concurrently running workers is one of the hyper-parameters. Besides that, this algorithm does not support minimum-quality criteria and instead of trying to find true solutions, its workers search for partial definitions, i.e., descriptions that cover none or just a few of the negative examples and at least one positive example. The maximum possible proportion of all negative examples covered by a partial definition is ParCEL's solution criterion. If a concept is marked as a partial definition, it is also excluded from the set of refinements added to the search tree. Furthermore, rather than returning the set of partial definitions (the solutions set in Algorithm 1) this algorithm merges them together into a single disjunction, which we call a generalization process. While focusing on partial definitions helps to fulfill the condition 3.2 from Definition 17, the subsequent generalization deals with the problem of satisfying the property 3.1 to some extent, as a partial definition alone often covers only a handful of positive examples. Since disjunctions are introduced during generalization, the ρ operator is configured so that it does not produce refinements with disjunctions.

ParCEL-Ex [24] is a modification of ParCEL that requires the partial definitions to cover solely positive examples, so no solution criterion can be specified. Moreover, ParCEL-Ex records counter-partial definitions as well, i.e., the partial definitions of negative examples. Anytime a refinement is processed that is neither a partial nor a counter-partial definition, the algorithm tries to combine this refinement with some of the negated counter-partial definitions into a conjunction in order to create a partial

definition. By appending the negations of counter-partial definitions, all the negative examples covered by any of these counter-partial definitions are removed from the set of negative examples that particular refinement covers. Although the combination can be postponed to happen after the entire search ends, the version 2 of ParCEL-Ex that we decided to employ performs it on-the-fly as described above. This method is suitable for situations in which a large search tree is expected to be generated. Due to the use of negations in combination, the ρ operator is further banned from producing refinement in which negated concepts occur.

Chapter 4

Data and Representation

Our aim is to characterize malware targeted at the family of Windows operating systems. Therefore, we begin this chapter with a brief overview of the Windows-specific Portable Executable format. Then, we present the SOREL-20M dataset as the source of malicious- and benign-software examples for our experiments. In the end, we discuss the PE Malware Ontology, which we used during data preprocessing that was inevitable for us to be able to supply the learning algorithms with semantic input.

4.1 Portable Executable Files

The Portable Executable (PE) standard [5] defines a common format for executables (EXEs), dynamic link libraries (DLLs), and object files in modern Windows operating systems, starting with Windows NT. The PE format extends the ubiquitous Common Object File Format (COFF) [22], initially introduced to unify the structure of executable, object, and shared-library files in Unix-based operating systems. The basic organization of a PE file is shown in Figure 4.1. We shortly describe its constituent parts below.

The MS-DOS header is a legacy header added purely for compatibility with MS-DOS 2.0 and newer, as well as earlier versions of Windows [7]. For this reason, we omit the details about the information it contains.

The MS-DOS stub can be found only in PE image files, i.e., EXEs and DLLs. It is an MS-DOS program which outputs a warning message saying that that image cannot be run in DOS mode when a user tries to run a PE image in an MS-DOS environment.

The **PE signature** is a string of four bytes indicating that the file is an image file in the PE format. This field is not present in PE object files.

The **COFF** file header contains details about the class of machines for which the file is targeted, the total number of sections in the file, the size of the optional header that follows, the file's type (e.g., EXE or DLL), and more.

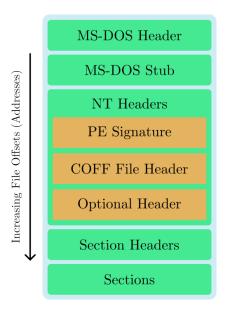


Figure 4.1: Simplified structure of a PE file.

The **optional header** has received its name on the grounds of the fact that it is used exclusively in image files. If present, this header provides us with further information about the file, such as linker version, address of the entry point, image base, data directories etc. Here, we focus on the data located in and referred to by data directories since they are the most relevant for our use case. Each of these directories act as a pointer to a table, a group of related tables, or a string with the actual data. Normally, every table (or group) resides in a separate section. The contents of the most notable tables are summarized in Table 4.1.

The array of **section headers** stores the key characteristics of all the sections in the PE file. For every section, there is a dedicated header bearing information about the section's name, entropy (a degree of randomness in the section's data), the type of the data it contains (code, initialized data, uninitialized data), access permissions (whether it can be read, modified, executed, or shared among multiple processes), etc.

4.2 SOREL-20M

The SOREL-20M dataset [14] is one of the first public large-scale datasets for static malware analysis. This dataset is composed of almost 20 million samples amassed from the beginning of 2017 until the middle of 2019, each representing either a malicious or a benign PE file (EXE or DLL). Alongside PE metadata extracted directly from the binary files, SOREL-20M contains format-agnostic data useful for malware analysis.

For each of the samples with PE metadata available (approx. 98% of all samples), there is a JSON object holding all the information in the headers and data-directory tables of the corresponding PE file, except for the actual certificates, fonts, graphics,

4.2. SOREL-20M 25

Table	4.1:	Contents	of	data-d	lirectory	tab.	les.
-------	------	----------	----	--------	-----------	------	------

Table(s)	Description of Contents		
Import Tables	identifiers of imported functions, constants, etc. and the		
	respective DLLs from which they should be imported		
Export Tables	public identifiers of exported functions, constants, etc. and their		
	respective addresses		
Resource Table	fonts, graphics and other file resources		
Certificate Table	certificates indicating that the file is digitally signed		
Base Relocation	pointers to addresses which need to be relocated if the image is		
Table	loaded at a base address different form the desired		
Debug Table	debug information (symbols, line numbers, strings, etc.)		
TLS Table	information on how to initialize and clean up thread-local storage		
	$(TLS)^1$		

and other resources.

The format-agnostic data are provided for each sample. This data include:

- the date and time the file associated with a given sample was first detected,
- the total number of times the file was seen in the span of data collection, and
- for malicious binaries only, a list of malware categories into which it may belong, such as adware, spyware or ransomware, as hinted by the results of behavioral analysis.

Besides SOREL-20M, there are very few datasets for static PE-malware analysis, for example, Microsoft Malware Classification Challenge Dataset [19], BODMAS [25], and EMBER [1], the majority of which does not include such comprehensive information about PE files extracted from headers. The EMBER dataset is an exception to this and hence, the previous experiments were carried on data from EMBER. As we were looking for an alternative source to validate the studied approach, we selected SOREL-20M for being largely compatible with EMBER and relatively up to date, which together with its extraordinary size allows for creating a realistic picture of the current state of the PE-malware world with much of the diversity captured.

¹Thread-local storage is a special kind of static (automatic) memory local to each thread. The data in this memory are initialized before a thread starts and emptied on its termination.

4.3 PE Malware Ontology

Since our approach uses concept learning requiring semantic input, the data from SOREL-20M need to be first transformed into a knowledge base or, as in our case, into an ontology. We decided to base this ontology on the PE Malware Ontology [21], which defines a class hierarchy and both object- and data-property hierarchies² suitable for static malware detection. The main reason behind this choice is the fact that the PE Malware Ontology is an extended and refined version of the ontology used in the proof-of-concept work whose outcomes we aim to validate and that to the best of our knowledge, no other relevant ontology for analysis of malicious software was published at the time of conducting this research.

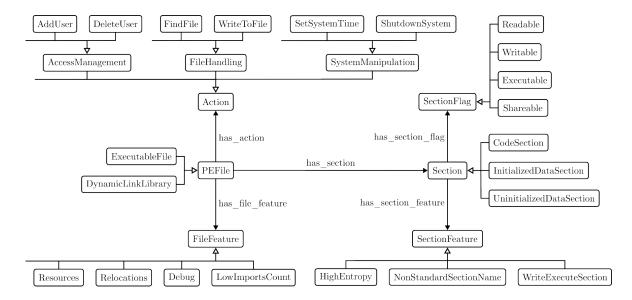


Figure 4.2: Core structure of the PE Malware Ontology. Class names are enclosed in rounded boxes. The fact that C is a direct subclass of D is represented by an unfilled arrow beginning at C and pointing towards D. A free end of a subclass-relation arrow indicates that there are more subclasses of that particular class which are not shown in the figure. A filled arrow connects the domain of the object property whose name is given above or next to that arrow to the property's range.

Figure 4.2 depicts the core structure of the PE Malware Ontology. Below, we describe the class hierarchy and the available object properties by going through all the most-generic classes (direct subclasses of owl:Thing).

PEFile. This class is meant to represent all instances of PE files that are in the ontology. We distinguish between EXEs and DLLs, for which there are two separate subclasses of PEFile – ExecutableFile and DynamicLinkLibrary, respectively.

²Here, by *hierarchies*, we mean the orderings induced by \sqsubseteq on the sets of class names, object-property names and data-property names, respectively.

FileFeature. The subclasses of the FileFeature class symbolize features of PE files that are interesting from the perspective of malware analysis, such as, the presence of a data directory (e.g., Resources and Relocations), the fact that the file's entry point lies within a non-executable section (NonexecutableEntryPoint), or that the file contains COFF debug symbols (Symbols). For each of the features a given PE file has, a link between the associated PEFile instance and the prototypical instance of the relevant FileFeature subclass is created using the has_file_feature object property.

Action. This class is the root of a three-level hierarchy of action-related classes. At the first level, there is the class Action. The second level consists of the direct subclasses of Action, which can be conceived of as action categories, e.g., FileHandling and Networking. Finally, the classes at the third level, i.e., the subclasses of the action-category classes, represent individual actions PE files may take, especially those that are potentially harmful, for example, FindFile and CreateSocket. The set of actions to which a PE file has access is inferred from the list of imports. To indicate that a PE file can perform a certain action, the corresponding PEFile instance and the representative of that particular action are connected through the has_action object property.

Section. In the PE Malware Ontology, each section of a PE file is also supposed to be modeled as an instance. The role of the Section class is to group together all these section instances. Similarly to PEFile, Section is further divided into three subclasses, CodeSection, InitializedDataSection, and UninitializedDataSection, to differentiate between sections based on the type of data they contain. A PE file (PEFile instance) is linked to its sections (Section instances) via the has_section object property.

SectionFlag. Section flags are simply access permissions, for which there are dedicated subclasses of the SectionFlag class: Readable, Writable, Executable, and Shareable. When a section has a particular flag, it is signified with the help of the has_section_flag object property the same way the connections between PEFile and FileFeature instances are created.

SectionFeature. The subclasses of SectionFeature enable us to record some purportedly valuable attributes of a section, e.g., high entropy (HighEntropy). Once again, the fact that a section has a given feature is signalized by defining a relationship between the corresponding Section instance and SectionFeature instance (the only instance of the matching SectionFeature subclass) through the has_section_feature object property.

The object-property hierarchy consists only of the already presented properties, all

of which are direct subproperties of owl:topObjectProperty.

As mentioned earlier, there are also several data properties declared in the PE Malware Ontology, for instance, to store a section's name, exact value of entropy, or the number of imported/exported symbols for a PE file. However, since we do not utilize the data properties throughout our experimentation, we will not discuss the data-property hierarchy any further.

Chapter 5

Implementation Changes

Prior to beginning the experimentation described later in Section 6, we made several modifications to the implementation of the official distribution of DL-Learner to improve the performance of the examined learning algorithms and resolve a couple of issues that arouse as we were performing preliminary tests. The updated version of DL-Learner which we used in our experiments can be downloaded from our GitHub repository¹. In this chapter, we discuss the most pivotal changes.

5.1 Refinement Operator

5.1.1 At-Most Restrictions

After noticing some inexplicable differences in the accuracy of two logically equivalent descriptions reported by OCEL (for the definition of accuracy, see Section 6.2), we found out that the ρ refinement operator was handling at-most restrictions inappropriately. More specifically, we realized that the operation

$$< n \ r.D \rightsquigarrow < n \ r.E,$$
 (5.1)

for any concept D, any role $r, n \in \mathbb{N}$, and $E \in \rho_{\operatorname{ar}(r)}(D)$, does not produce downward refinements. Moreover, this operation actually generates upward refinements if we assume that $E \sqsubseteq D$, which is expected to be satisfied for a downward refinement operator like ρ . We verify our claims by proving Lemma 1 below.

Lemma 1. Let \mathcal{L} be a DL language which allows cardinality constraints and \mathcal{K} be a knowledge base in \mathcal{L} . Let n be a natural number, $r \in \mathbf{R}^s$ be a role, and D, E be such concepts from \mathbf{C} that $E \sqsubseteq D$. Then, the operation

$$\leq n \ r.D \iff \leq n \ r.E,$$
 (5.2)

is an upward refinement operation.

¹https://github.com/mousetom-sk/DL-Learner/tree/v3

Proof. Let \mathcal{L} be a DL language which allows qualified number restrictions and \mathcal{K} be a knowledge base in \mathcal{L} . In order to prove that (5.2) is an upward refinement operation, it is now sufficient to show that for all concepts $D, E \in \mathbf{C}$ such that $E \sqsubseteq D$, all roles $r \in \mathbf{R}^s$, and any $n \in \mathbb{N}$, the proposition $\leq n \ r.D \sqsubseteq \leq n \ r.E$ holds, i.e., that for every model \mathcal{I} of \mathcal{K} it is also true that

$$\mathcal{I} \models < n \ r.D \ \Box < n \ r.E. \tag{5.3}$$

Therefore, let D and E be arbitrary concepts in \mathbb{C} with $E \sqsubseteq D$, let $r \in \mathbb{R}^s$ be an arbitrary role, and let n be a natural number. Let us further take an arbitrary model \mathcal{I} of \mathcal{K} . As we aim to prove (5.3) which holds if and only if $(\leq n \ r.D)^{\mathcal{I}} \subseteq (\leq n \ r.E)^{\mathcal{I}}$, we first construct the sets $(\leq n \ r.D)^{\mathcal{I}}$ and $(\leq n \ r.E)^{\mathcal{I}}$ based on the definition of the interpretation function:

$$(\leq n \ r.D)^{\mathcal{I}} = \{ a \in \Delta^{\mathcal{I}} \mid |\{ b \in \Delta^{\mathcal{I}} \mid (a,b) \in r^{\mathcal{I}} \text{ and } b \in D^{\mathcal{I}} \} | \leq n \},$$

$$(\leq n \ r.E)^{\mathcal{I}} = \{ a \in \Delta^{\mathcal{I}} \mid |\{ b \in \Delta^{\mathcal{I}} \mid (a,b) \in r^{\mathcal{I}} \text{ and } b \in E^{\mathcal{I}} \} | \leq n \}.$$

Taking into account our premise that $E \sqsubseteq D$, we can also conclude that for any $b \in \Delta^{\mathcal{I}}$, it has to be true that if $b \in E^{\mathcal{I}}$, then $b \in D^{\mathcal{I}}$, since $E \sqsubseteq D$ iff $E^{\mathcal{I}} \subseteq D^{\mathcal{I}}$. Consequently, the inclusion

$$\{b \in \Delta^{\mathcal{I}} \mid (a, b) \in r^{\mathcal{I}} \text{ and } b \in E^{\mathcal{I}}\} \subseteq \{b \in \Delta^{\mathcal{I}} \mid (a, b) \in r^{\mathcal{I}} \text{ and } b \in D^{\mathcal{I}}\}$$

and the corresponding inequality

$$|\{b \in \Delta^{\mathcal{I}} \mid (a,b) \in r^{\mathcal{I}} \text{ and } b \in E^{\mathcal{I}}\}| \leq |\{b \in \Delta^{\mathcal{I}} \mid (a,b) \in r^{\mathcal{I}} \text{ and } b \in D^{\mathcal{I}}\}|$$

must be satisfied for any $a \in \Delta^{\mathcal{I}}$. Thus, when an individual $a \in \Delta^{\mathcal{I}}$ belongs to $(\leq n \ r.D)^{\mathcal{I}}$, it has to be an element of $(\leq n \ r.E)^{\mathcal{I}}$ as well, because given such $a \in \Delta^{\mathcal{I}}$, from our previous observations it follows that

$$n \ge |\{b \in \Delta^{\mathcal{I}} \mid (a, b) \in r^{\mathcal{I}} \text{ and } b \in D^{\mathcal{I}}\}|$$

$$\ge |\{b \in \Delta^{\mathcal{I}} \mid (a, b) \in r^{\mathcal{I}} \text{ and } b \in E^{\mathcal{I}}\}|.$$

This brings us to the desired conclusion that $(\leq n \ r.D)^{\mathcal{I}} \subseteq (\leq n \ r.E)^{\mathcal{I}}$.

Refining at-most restrictions through the operation (5.1) is thus not in accordance with the intention to design ρ as a downward refinement operator. To cope with this problem, we redefined this operation as follows:

$$\leq n \ r.D \leadsto \leq n \ r.(\neg E),$$
 (5.4)

i.e., we inverted the direction in which the constrained concept is refined (from downwards to upwards). With the help of Lemma 1, it can be easily shown by the principle

of structural induction for the selected language \mathcal{L} that when we change (5.1) to (5.4) in the definition of ρ , the ρ operator becomes a downward refinement operator. The key is to leverage the fact that the validity of Lemma 1 also implies that the inverse of (5.2) is an operation of specialization.

Of course, this modification also requires the refinement process of at-most restrictions to start from the concept $\leq n \ r. \perp$ instead of $\leq n \ r. \top$ as in Definition ...

5.1.2 Negations And Universal Quantification

Studying the definition of the ρ refinement operator more carefully, we later detected at least two other places for potential improvement.

Fristly, we prevented the operator from generating the concept-negation refinements having the form $\neg C$, where $C \in \mathbf{C}$ is a super-concept of the domain in which the refinement is performed, for instance, the range of a role. Clearly, this does not decrease the expressive power of the operator because such negations cannot cover any individual from the given domain, yet it helps to reduce the number of nodes in the search tree.

Secondly, we decided to shorten the refinement path from the top concept to the universal quantification concepts of the following kind: $\forall r.\bot$. Originally, a concept $\forall r.C$, with $C \in N_C$ a most-specific concept name, i.e., one for which no $D \in N_C$ exists such that $D \sqsubseteq C$, had to be reached in order to produce $\forall r.\bot$ (see Definition 22). Proceeding in this manner, we could observe a phenomenon that $\forall r.\bot$ is never introduced during refinement, which may happen if, for example, the universal quantifications with most-specific concept names are not promising enough to be further refined. We think that $\forall r.\bot$ should be searched irrespective of whether a universal quantification of r with some most-specific concept name is valuable, as it bears a slightly different meaning, e.g., in our context, \forall has_section_feature. \bot represents all sections with none of the special features. Contrarily, a concept of the form $\forall r.\bot$ could also quite unnecessarily appear multiple times in a search tree because it was a refinement of every concept $\forall r.C$, where C is most-specific. To address these issues, we redefined the ρ operator in a way that makes $\forall r.\bot$ a direct refinement of $\forall r.\top$.

5.1.3 "Some-Only" Rule

Although the formal definition of ρ is strict, its implementation in DL-Learner is largely configurable. One of the options allows us to control the use of the "some-only" rule. If this rule is applied, a universal quantification of a role can occur in a refinement only in conjunction with an existential quantification of the same role. For example, the descriptions of the form $(\forall r.C) \sqcup D$, for any $C, D \in \mathbf{C}$ and $r \in \mathbf{R}$, would be considered invalid, but a concept such as $(\exists r.E \sqcap \forall r.C) \sqcup D$, with any $E \in \mathbf{C}$ not disjoint from C, would be accepted. Taking this precaution precludes the algorithms from over-fitting

when no negative example that does not have any r-filler is seen during learning, in which case, the first example description covers exactly the same set of individuals as the second while being significantly shorter and thus preferred by each algorithm.

We extended this rule by permitting a universal quantification in conjunction with an at-least restriction as well since semantic-wise, at-least restrictions are just more constrained existential quantifications.

5.2 Reasoner Component

5.2.1 Cardinality Constraints in the Closed-World Reasoner

Redefining the ρ operator as suggested in Section 5.1.1 did not settle all the problems with accuracy. We discovered this while comparing the output of OCEL and CELOE, which disagreed in the accuracy of the same concepts containing at-most restrictions. After further investigation, we came to the conclusion that the problem was caused by the employed closed-world reasoner, which was not always answering the queries asking whether a certain individual belongs to the extension of a given concept with cardinality constraints correctly due to simple programmatic errors.

This problem was fixed by rectifying the implementation of the closed-world reasoner.

5.2.2 Concurrent Closed-World Reasoner

The aforementioned closed-world reasoner provided in DL-Learner allows us to configure its behavior in several ways. For example, we can choose between instance-based and explicit checks of concept disjointness, that is, whether to infer the disjointness of two concepts from the fact that they have no instance in common, or to rely solely on the available concept-disjointness axioms and the information on disjointness they entail.

Experimenting with the parallel algorithms, we noticed that when opting for the second method some worker threads terminated due to an unexpected concurrent modification of the reasoner's internal data structures. We deduced that this was a consequence the fact that all workers were consulting the same reasoner instance.

To resolve this issue, we first tried creating one standalone copy of the closed-world reasoner for each worker but this solution was causing a bottleneck in the early phases of learning since each copy had to be initialized separately. As a remedy to this problem, we thus eventually implemented a concurrent closed-world reasoner maintaining a pool of the original (base) closed-world reasoners sharing the read-only internals whose construction demands the majority of time during initialization.

5.3 Heuristic in OCEL

As mentioned in Section ..., OCEL uses a heuristic to determine which parts of the search space to explore first. The role of one undocumented component of this heuristic function was to encourage the algorithm to refine concepts containing $\forall r. \top$ or $\leq n \ r. \top$ by artificially bettering their heuristic score. Such concepts might be interesting for further refinement due the fact that $\forall r. \top$ is logically equivalent to \top and that $\leq n \ r. \top$ is usually too broad, which means that on their own, they provide no or only little information. In addition, $\forall r. \top$ and $\leq n \ r. \top$ were the starting points on the paths to all universal-quantification and at-most-restriction refinements for the role r, respectively, so, naturally, there is a greater potential to replace these less informative expressions with some more specific ones through refinement. A clear advantage of their refinement is that we can gain the extra expressivity without much increase in the length and complexity of the whole concept.

However, the implementation of this component of the heuristic was not deterministic and the adjustment to the final score did not grow with each occurrence of any of the above two expressions in the evaluated concept, which we consider crucial for a proper assessment of a concept's capacity to specialize. Moreover, after the changes presented in Section 5.1.1, it makes more sense to favor $\leq n \ r.\bot$ rather than $\leq n \ r. \top$, as it is the former that now begins every refinement chain of at-most restrictions on r.

Hence, we altered this part of OCEL's heuristic to ensure that its output is deterministic, that the final score correction accumulates with the increasing number of appearances of the expressions in question, and that it supports the refinement of concepts containing $\leq n \ r.\bot$ instead of those with $\leq n \ r.\top$.

5.4 ParCEL and ParCEL-Ex

5.4.1 Same-Length Refinements

When refining a concept expression via the ρ operator, both parallel algorithms, or at least their implementations in DL-Learner, required the direct refinements to be longer than the expression from which they resulted. Apparently, this was not the intention of the authors, since it deprives the algorithms of many valuable concepts. For instance, the descriptions of the form $\forall r.C$, with $C \neq \top$, were completely unreachable with this restriction imposed because the only path to them leads through $\forall r.\top$, of which they are direct refinements but with no greater length.

We resolved this issue by allowing ParCEL and ParCEL-Ex to accept also those direct refinements whose length is equal to the length of the refined concept.

5.4.2 Accuracy Calculation in ParCEL

The process of calculating the accuracy of a concept expression for the purposes of ParCEL's heuristic and determining if the concept is a partial definition was originally taking into account the coverage of the hitherto found partial definitions as well. More specifically, the positive examples covered by the already learned partial definitions were excluded from the set of positive examples considered during the calculation. We suppose that the rationale behind this change to the standard definition of accuracy was to promote those expressions that can potentially contribute to the overall coverage of all positive examples the most, which is a reasonable goal to strive for. Nevertheless, the way this objective was attained brought a bit of uncertainty into the selection of concepts for refinement, possibly developing a preference for otherwise less suitable concepts, as under these circumstances, the accuracy reflects not only the actual quality of a concept from the global viewpoint, but also when it was evaluated. This would require us to recompute the accuracy of each searched concept every time a new partial definition is found to always have an up-to-date measurement of their aptitude for refinement. Despite that, the calculation was performed only at the time of the discovery of a given concept by virtue of being a resource-intensive task.

Therefore, we decided to re-implement the procedure of accuracy calculation so that the basic definition, provided in Section ..., is used. In order to draw the algorithm's attention to the promising concepts, we added the following rules. When a node of the search tree is revisited to seek for new refinements, we first check whether the concept it represents still covers at least one positive example that is not an instance of any of the already found partial definitions. If no such example exists, the node is removed from the search tree and the corresponding concept is never refined again. Likewise, a description now needs to cover strictly more of the yet uncovered positive examples than uncovered negative examples in order to be deemed a partial definition.

5.4.3 Acceleration of Accuracy Calculation

Previously, the accuracy of a concept was always calculated from scratch in ParCEL and ParCEL-Ex. Inspired by the implementation of OCEL, we sped up this calculation by keeping and exploiting the information on which positive and negative examples are covered by the searched concept expressions. These data are stored in the respective nodes of the search tree. To compute the accuracy of a given concept's refinement, it is then sufficient to determine what subsets of positive and negative examples covered by the original concept are also covered by that particular refinement because we know that ρ is a downward refinement operator, and thus each refinement can cover only the examples covered by its direct predecessor. In combination with other enhancements, this modification enabled the parallel algorithms to triple the number of concept ex-

pressions they were able to search per unit of time, which also forced us to devise a compressed representation of the sets of the covered examples to fit the entire search tree into the available memory.

Motivated by this rise in the number of searched expressions, we tried to improve the performance of CELOE in a similar manner. However, our experiments showed that CELOE can barely benefit from the accelerated accuracy calculation and that the necessary compression and decompression sometimes even outweighs the effects of the more efficient computation of accuracy in terms of time consumption. We assume that this stems from the fact that CELOE endeavors to find a single description as a whole, whereas the parallel algorithms search for partial definitions that often cover significantly less examples so much more time is saved with this optimization of accuracy calculation. OCEL, which uses this technique out of the box, copes with the problem of the enlarged search tree by means of periodic branch pruning in place of compression. Since this would be a quite fundamental intervention in the implementation of CELOE, we eventually decided not to alter the way CELOE computes accuracy.

5.4.4 Search Tree Organization

Although the change we discuss in this section is a bit more technical when compared to the ones mentioned above, we find it important to present it here due to its surprisingly immense impact despite its simplicity.

The problem we are about to describe consisted in how the search tree was accessed and maintained by ParCEL and ParCEL-Ex. Both investigated parallel algorithms use Java's ConcurrentSkipListSet to store all the nodes of the search tree in the order determined by the values assigned to the concepts they embody by their heuristics. Previously, each time ParCEL or ParCEL-Ex was ready to refine a concept expression it polled the last element of this set – the node with the currently best concept according to the heuristic.

In our efforts to make the search tree representation more compact, induced by the modification proposed in Section 5.4.3, we noticed that the official documentation for ConcurrentSkipListSet emphasizes that ascending iterators over this data structure allows faster access than the descending iterators. Therefore, we closely examined the difference in the time required to empty a set of this type by repeatedly polling the last element versus the first. As retrieving the first element proved to be on average almost two times faster during our tests, we reversed the order of nodes in the search tree and instructed the algorithms to poll the first element instead of the last. It also has to be noted that storing the elements in the reversed order does not affect the insertion time.

Chapter 6

Experiments

In this chapter, we describe our experimentation process in detail. We expand upon the conditions under which we evaluated the performance of the learning algorithms, including the input data we prepared, what methodology we used for performance evaluation, and what configurations of the algorithms were tested.

6.1 Test Cases and Ontology Preparation

We performed our experiments in three settings differing in the nature of input data.

6.1.1 Test Case 1 – Mixed Data

In the first test case, we studied the capabilities of the learning algorithms in the most general situation where no prior categorization of samples takes place.

For the purposes of this test case, we prepared four mutually disjoint datasets. Each dataset consists of 1000 samples evenly split between malicious and benign, as well as EXEs and DLLs (see Table 6.1). These samples were selected from the entire SOREL-20M dataset at random. The decision on dataset size was largely affected by the time and memory requirements of the algorithms and the resources we had at our disposal. Augmenting the PE Malware Ontology by adding the knowledge about the extracted samples, we then created the ontology that was later provided to the learning algorithms together with the information on which samples should be treated as positive and which as negative – in our context, malware and benign-software samples, respectively.

In reality, the number of benign-software samples exceeds the number of malware samples by an order of magnitude, usually, 80 benign binaries are observed per each piece of malware that appears [18]. In spite of that, we were encouraged to balance the datasets in this regard because with a dataset of 1000 samples, ensuring even a 10% share of malware does not have to sufficiently motivate the algorithms to learn as

File Type	Malicious	Benign
EXE	250	250
DLL	250	250

Table 6.1: Number of malicious/benign samples by file type in the mixed datasets.

in such a case, it is still enough to precisely cover a few malicious samples to achieve a favorable heuristic score due to high accuracy (we define accuracy in Section 6.2). Moreover, our goal is to also find descriptions that can discriminate malware from benign software in general, which is hardly possible when we give the algorithms only a limited amount of information on features of malicious binaries, lacking diversity.

Likewise, we did not want the algorithms to learn that the chance a file of a certain type is harmful is too low to bother describing it. To this end, the one-to-one ratio of EXEs to DLLs among both the malicious and benign samples was established. We think that taking this step was particularly important for the objectivity of the obtained results. We hold this opinion because of our experience with undesirable results in an unbalanced setting. Initially, we constructed one dataset of 500 malicious and 500 benign samples randomly drawn from SOREL-20M without any restrictions on the proportion of EXEs to DLLs. Inspecting this dataset, we discovered that only about 20% of all samples were DLLs and that malicious DLLs barely accounted for 10% of all DLLs in this dataset. The algorithms were able to achieve high accuracy but merely in the wake of the scarcity of malicious DLLs and the fact that the expressions they found were covering mostly EXEs.

Finally, it has to be noted that we also added a number of axioms to the resulting ontology to explicitly express the obvious fact that each class in the PE Malware Ontology is disjoint from every other class therein, with the exception of the subclasses of the class Section. We refrained from asserting disjointness here because we noticed that it is possible to attach multiple content-type labels to a PE-file section. As this is unusual, it may be an indication of malware as well. We further clarify why we introduced these class-disjointness axioms in Section 6.3.

6.1.2 Test Cases 2 and 3 – Separation of Concerns

The test cases number 2 and 3 are tightly related to one another because in the former, we let the algorithms to focus exclusively on EXE binaries while in the latter, they were only confronted with DLLs. We expected that learning the attributes of malicious EXEs and DLLs separately could yield better results as finer descriptions might be found. Furthermore, having to characterize both at once may overload especially the

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non-parallel algorithms, i.e., OCEL and CELOE, which try to find a description as a whole rather than producing it in a distributed manner, for example, through partial definitions. OCEL and CELOE thus almost necessarily have to search for disjunctions with one disjunct per file type but such concepts are inherently longer and less attractive for the learners. Additionally, since we are able to determine whether a file is an EXE or DLL directly by inspecting the file's metadata, we consider first finding out a file's type and then using a type-specific classifier a feasible approach to malware detection.

For each of these two test cases, we again created four non-overlapping datasets comprising 1000 samples. As mentioned above, each dataset for the second test case contains only the samples representing EXE files, of which 500 are malicious and 500 benign. Similarly, each dataset prepared for the third test case consists of 500 malicious and 500 benign DLL samples. The calibration and the first validation dataset for both of these test cases were constructed from the samples present in the datasets for the first test case. The other validation datasets are composed of randomly selected samples from the remainder of SOREL-20M.

The final ontologies provided to the learning algorithms were created as previously, i.e., by combining the PE Malware Ontology with sample data and class-disjointness axioms.

6.2 Evaluation

In each test case, we first investigated various configurations of the learning algorithms to optimize some hyper-parameter values as we describe in Section 6.3. Among the four datasets prepared for the corresponding test case, we reserved one (calibration) dataset for this stage, on which the performance of all configurations was evaluated. Then, we selected the overall best configurations of each algorithm and evaluated their performance on the other three (validation) datasets for that particular case. The purpose of this further validation was to counteract the smaller dataset volume and verify that similar results can be produced on broader range of data.

For the evaluation of each configuration, whether during the optimization or the subsequent validation stage, we employed k-fold stratified cross-validation [10]: With the dataset partitioned into k subsets (folds) of equal size preserving the original proportions of selected classes, k experiments are performed, each time leaving a different fold aside as the test set while using the remaining k-1 folds as the training set. We chose k=5 and our stratification resided in retaining the ratio of malicious samples to benign samples, as well as EXEs to DLLs within both categories in the first test case.

Experiments were run on two identical Ubuntu 20.04-1 machines with a 12-core AMD Ryzen 9 5900X CPU and 64 GB of RAM each. The duration of each experiment

was limited by a specified amount of time, which was the only termination criterion used, apart from finding a perfect solution (see Definition 17). For OCEL and CELOE configurations, we set this learning timeout to 2 hours of user time, i.e., the actual time the CPU spent executing the corresponding process. For ParCEL and ParCEL-Ex configurations, the time limit was ... to 24 hours of user time in the first test case and later reduced to 12 hours in the second and third test case, which ...

We decided to keep the time measurement relative to the utilization of CPU to ensure fairness regardless of the system load.

For evaluation purposes, we used the following standard metrics [12]:

$$accuracy = (TP + TN)/(P + N),$$

 $precision = TP/(TP + FP),$
 $recall = TP/P,$
 $specificity = TN/(FP + TN),$
 $FP \ rate = FP/N = 1 - specificity,$
 $F1 \ score = 2/(1/precision + 1/recall),$

where P(N) denotes the total number of positive (negative) samples, TP(FP) denotes the number of positive (negative) samples classified as positive, and TN(FN) denotes the number of negative (positive) samples classified as negative.

6.3 Tested Configurations

We identified several hyper-parameters of the studied learning algorithms that we presumed can potentially impact their performance. These parameters were subject to optimization throughout our experimentation in each test case. However, before we delve into the details, we present the modifications we made to the default configuration of the algorithms which were applied in all experiments.

Firstly, we instructed the algorithms to seek refinements exclusively in the domain of PEFile (the default is owl:Thing), i.e., to consider only those class descriptions which are subsumed by PEFile when searching for solutions. This means that the expressions which cannot characterize any (malicious) PE file, such as CodeSection \Basssection_flag.Readable, do not appear in the search space on their own, which helps the algorithms to learn more efficiently. Next, we changed the process of determining whether two classes are mutually disjoint form being instance based to being based on explicit assertions, since we think that class disjointness should not be deduced from the instance data, but rather from the general knowledge about the classes, hence also the need for the supplementary class-disjointness axioms. To make the learning easier, we forbade the use of data properties as mentioned earlier. For the purposes of

instance checking, OCEL and CELOE were provided with the corrected closed-world reasoner, while ParCEL and ParCEL-Ex were requested to consult the new concurrent version of this reasoner. We set up both reasoners to use the standard semantics of universal quantification because by default, $\forall r.C$ is interpreted as $\forall r.C \sqcap \exists r.C$, resulting in an implicit application of the "some-only" rule, with which we decided to experiment during the hyper-parameter optimization. In order to spare computing time, we disabled the simplification of class expressions in the set of solutions based on logical equivalence, for example, $(C \sqcup D) \sqcap E$, where $C \sqsubseteq D$, would be transformed to $D \sqcap E$. This is normally performed by CELOE to output shorter and less complicated descriptions. Lastly, ParCEL and ParCEL-Ex were limited to 12 concurrent workers to fully exploit the benefits of parallelization w.r.t. the available resources (the number of CPU cores on the evaluation machines described in Section 6.2). With regard to this choice, we configured the concurrent closed-world reasoner to maintain a pool of 13 base reasoners, so that there is always at least one idle reasoner ready to handle incoming queries.

Now, we look at the hyper-parameters with which we were experimenting.

Noise. Noise represents the minimum-quality criteria for OCEL and CELOE, the solution criteria for ParCEL, and the termination criteria for ParCEL-Ex. The respective roles of these criteria were discussed in Section 3.2.2. In CELOE, noise directly translates to an upper bound for the percentage of the false-negative rate of a class expression that should be considered for further refinement, i.e., for such expressions, following must hold: $FN\ rate < noise/100$. OCEL's formula is more intricate but can be simplified to $FN\ rate < 2 \cdot noise/100$ in our case. For ParCEL, the noise value is the maximum percentage of the FP rate of a partial definition, so any expression has to satisfy the inequality $FP\ rate \le noise/100$ to be accepted as a partial definition. ParCEL-Ex treats noise as the FP-rate percentage of the entire disjunction of partial definitions which is enough to reach to terminate the learning process. Since we decided to stop learning after a specified a period of time, we did not calibrate the value of noise for ParCEL-Ex, leaving it always set to 0. Tweaking the value of noise, our goal was to optimize the level of FP rate in combination with other metrics.

Use of Negations. By means of this parameter, we can control the use of negations in the generated class expressions. Disallowing negations not only narrows the search space but we hypothesized that it may also encourage the algorithms to find expressions of higher quality, i.e., ∃has_action.(AddUser □ Encrypt) rather than ∃has_action.(¬DeleteUser), and reduce the number of negative test examples classified as positive, which the negated expressions are more likely to cover. Even though ParCEL-Ex was originally designed to work with negations disabled due to the introduction of counter-partial definitions, we studied the effects of enabling them on the

performance of ParCEL-Ex as well on account of the fact that ParCEL and ParCEL-Ex use the same heuristic, which is optimized for finding partial definitions only.

"Some-Only" Universal Quantification. In spite of the fact that the default behavior is to perform "some-only" checks (discussed in Section 5.1.3), which could prevent the algorithms from over-fitting ($\forall r.C$ covers all individuals which do not have an r-filler), we theorized that deactivating this rule might give the algorithms an access to valuable parts of the search space.

Restrictions on Cardinality Constraints. We experimented with two parameters restricting the construction of cardinality constraints – allowedRolesInCardinalityRestrictions and maxCardinalityLimit. With the former, we can define the set of properties that are allowed to be used to produce cardinality constraints. The latter represents an upper limit for the quantity in at-most restrictions. Our goal was to try to guide the search towards more explicit and simpler descriptions via these parameters. For example, ≤ 3 has_action.FileHandling is a relatively vague characterization of a PE-file category. Similarly, we assume that for an at-most restriction of the form $\leq n \ r.C$, where $n \geq 2$, to be a decent description, the complexity of C needs to be high. However, neither of these two parameters was included in the official distribution of DL-Learner and the support for them was implemented by us, taking an inspiration from the existing parameter for limiting the quantity in all cardinality constraints.

In order to test as much reasonable combinations of values for the aforementioned hyper-parameters, we split the experimentation into three phases. At the end of each phase, two configurations of each algorithm (one for each of the selected values of noise in the later phases) were chosen to proceed to the next phase.

In the first phase, we optimized the selection of noise. Regarding OCEL, we started with the value of 5, which we were gradually increasing by 5 until we stopped at the noise of 25. The first, the step, and the last value for CELOE were 10, 10, and 50, respectively. The second phase was devoted to investing the effects of disabling negations and "some-only" checks on the overall performance. Both were enabled in the first phase and here, we tested all the remaining combinations. In the last phase, we used the two newly-added parameters to control the generation of cardinality constraints either by allowing only the has_section object property to be constrained via cardinality constraints (hereafter also HS), or by limiting the maximum quantity in at-most restrictions to 1 (hereafter also M1). These rules were not applied in the previous phases.

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