## Advanced statistical physics Homework 2

first appeared on 8.4.2020, due 27.4.2020 by email to juraj.tekel@gmail.com

feel free to hand in solutions in slovak

**Problem 1** (Ups). Measurement of mass of a particle has given a result  $(-0.3 \pm 1)eV$ . This is clearly wrong since the mass has to be positive. What is the corrected result for the mass of the particle after taking this into consideration?

**Problem 2** (Canonical ensemble as density matrix.). The canonical ensemble can be viewed as a density matrix

$$\rho = \frac{1}{Z} e^{-\beta H} = \frac{1}{Z} \sum_{n} \left| n \right\rangle e^{-\beta E_{n}} \left\langle n \right| \; .$$

Using the expression for the entropy

$$S = -k \operatorname{Tr}\left(\rho \log \rho\right)$$

show that S = (E - F)/T.

**Problem 3** (Density of states.). What is the density of states for classical and ultra-relativistic particles in 2 and 1 dimensions?

**Problem 4** (Air-hockey equation of state.). What is the equation of state for the two dimensional system of hard pucks of radius R in a box of size  $L \times L$ , which takes into account first non-trivial contribution of their interaction?

**Problem 5** (Bonus. Hyper-hockey equation of state.). What is the equation of state four dimensional system of hard 4-spheres of radius R and a constant potential  $-V_0$  when separated by less than xR in a box of size  $L^4$ , which takes into account first non-trivial contribution of their interaction?