

# Vybrané kapitoly zo štatistickej fyziky

## Príklady z cvičenia

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7.5 Linear Response Theory and the Fluctuation–Dissipation Theorem

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**Príklad 1** (Exercise 7.4). Compute the dynamic susceptibility for a Brownian particle of mass  $m$  in the presence of white noise  $\xi(t)$  and fluid friction  $\gamma$ .

**Príklad 2** (Exercise 7.5). Verify the Kramers–Kronig relations for the dynamic susceptibility in Exercise 7.4.

**Príklad 3** (Exercise 7.6). Given the dynamic susceptibility  $\chi(\omega) = (-im\omega + \gamma)^{-1}$  for simple Brownian motion (see Exercise 7.4) and the thermal average  $\langle v^2 \rangle_T = kBT/m$ , use the fluctuation–dissipation theorem to obtain the velocity autocorrelation function.

**Príklad 4** (Exercise 7.7). Prove that  $\bar{\xi}(0) = \bar{g}^{-1}/T$ , where  $\bar{g}$  is the matrix whose matrix element is  $g_{ij} = (\partial^2 S / \partial \alpha_i \partial \alpha_j)_U$ .